

# Introduction to Cloud Modeling. Part VI: Types of Model

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introduction to process oriented modeling”  
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# Outline

- » Introduction
- » 0D 'parcel models'
- » 1D cloud models
- » 2D cloud models
- » 3D cloud models
- » Example of modeling system for research and forecasting
- » Summary



# INTRODUCTION



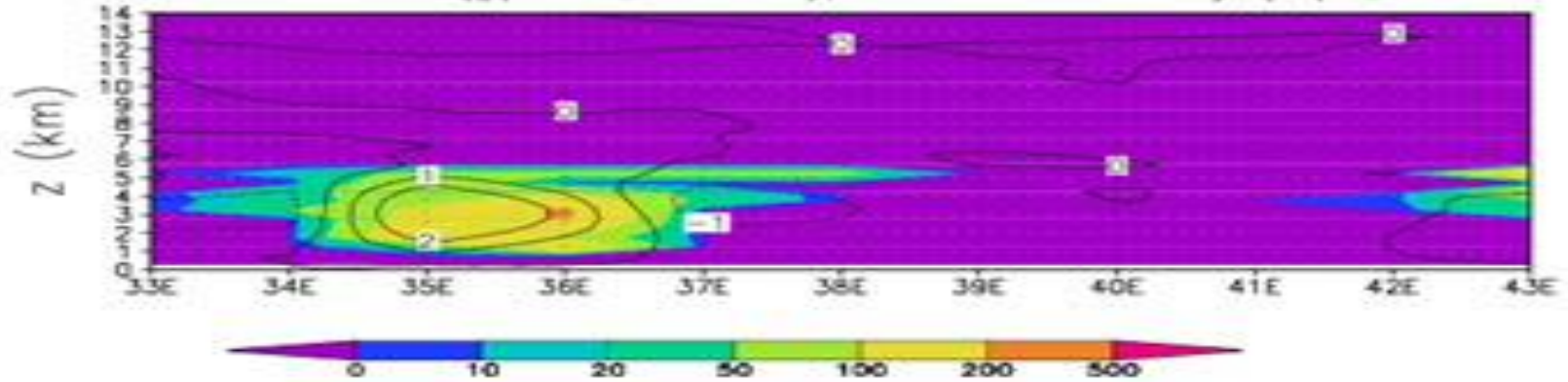
Diversity of models that predict cloud properties, with wide range of resolutions and of levels of detail



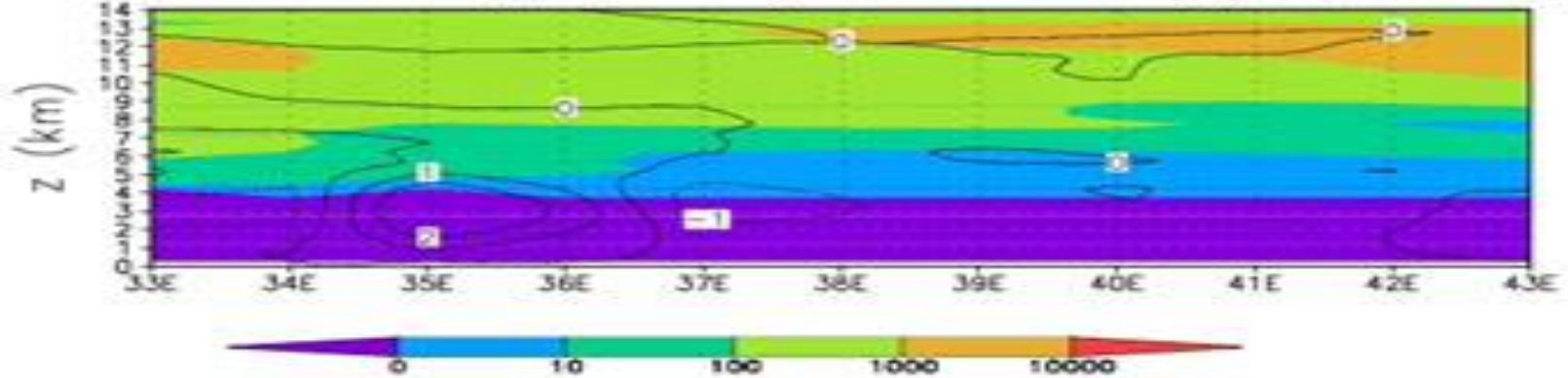
Example: High-resolution ( $dx = 2$  km) cloud-resolving model of aerosol-cloud interaction with 6 species of aerosol and 2-moment bulk microphysics (Phillips et al. 2009)



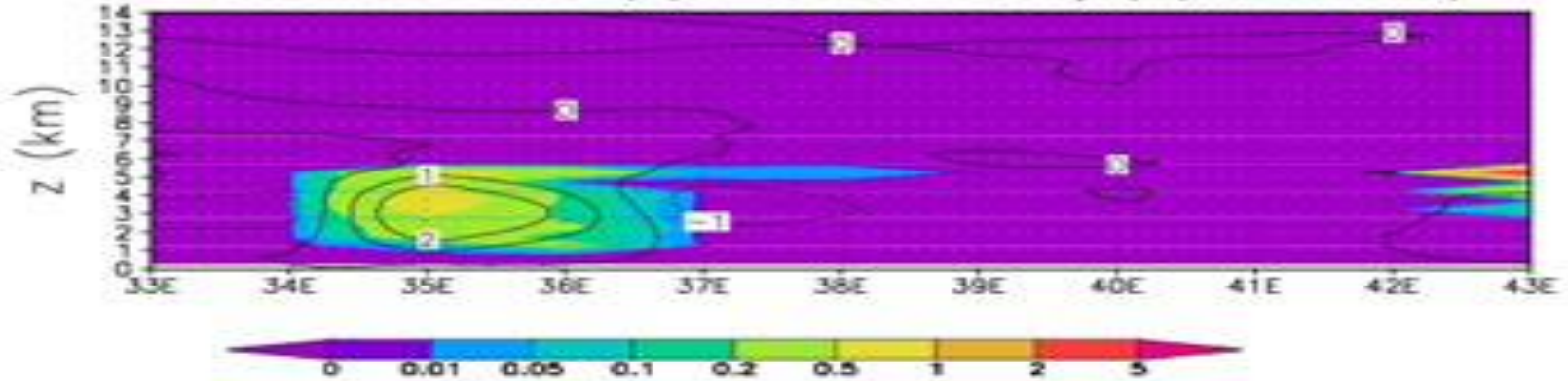
DROPLET NUMBER (#/cm<sup>3</sup>, shaded), vertical velocity (m/s, contours)



CRYSTAL NUMBER (#/L, shaded), vertical velocity (m/s, contours)

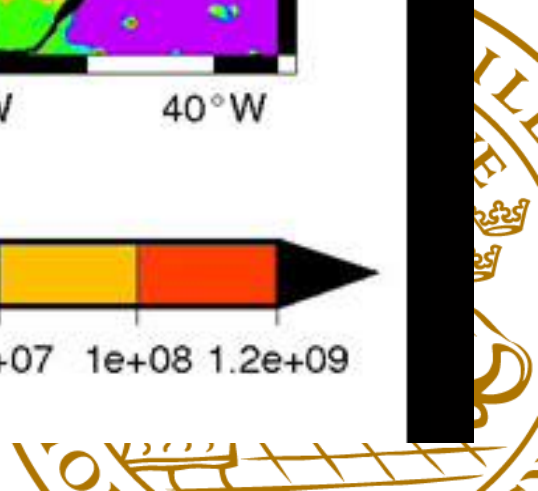
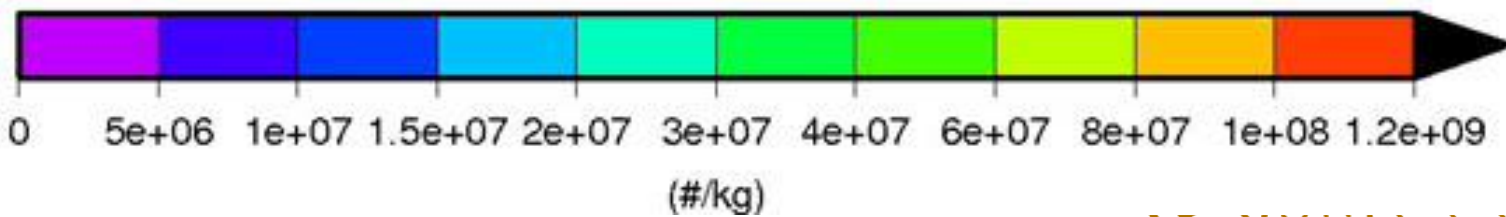
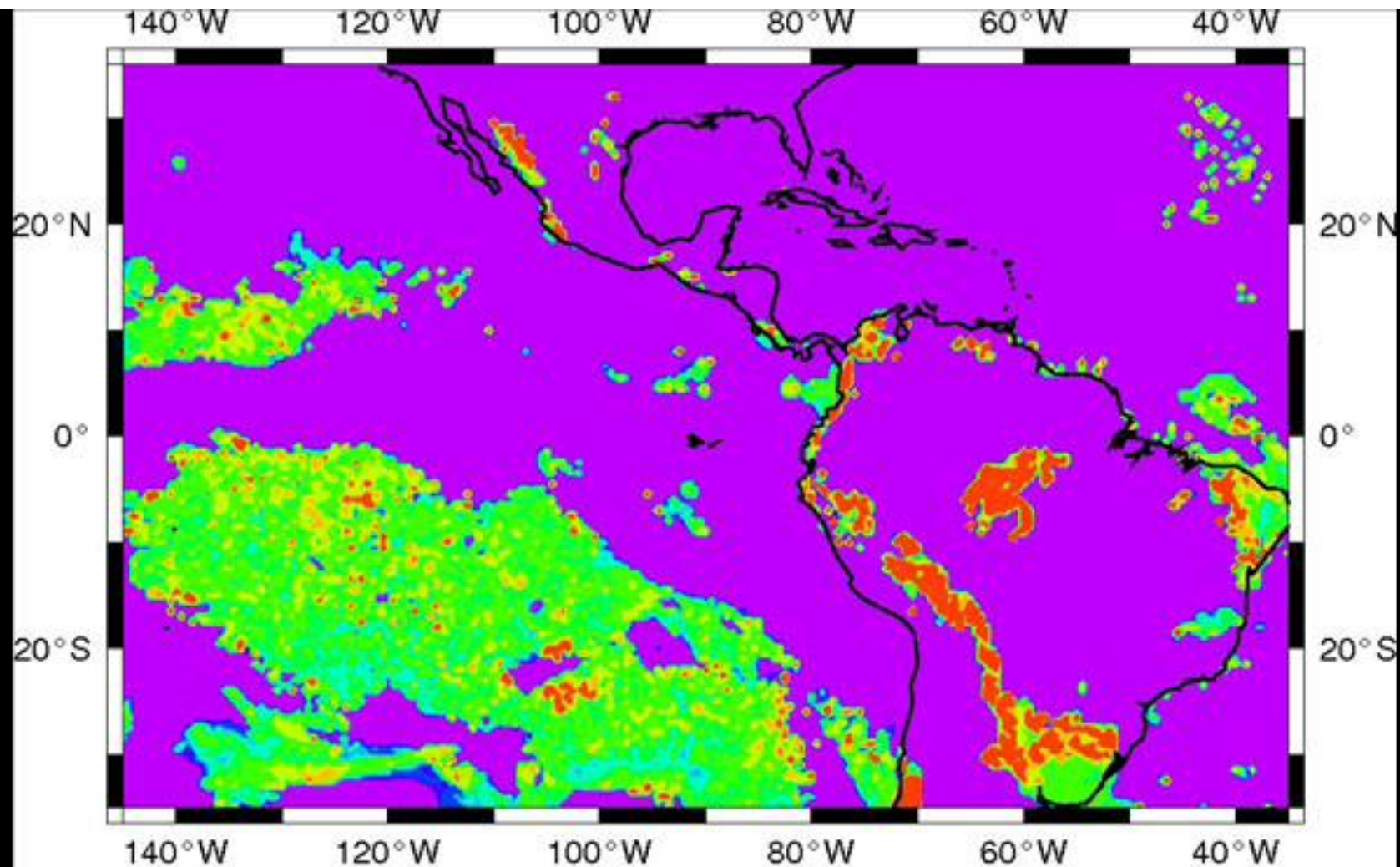


SUPERSATURATION (%), vertical velocity (m/s, contours)



Example: Regional model ( $dx = 50$  km) of Pacific and Americas, with similar Phillips scheme of aerosol-cloud interaction, for prediction of properties of large-scale clouds (Lauer et al. 2009)







# 0-D CLOUD MODELS



# 0D parcel models

- » Parcel = buoyant element of air with size and shape unspecified
- » Assumptions that parcel:
  - maintains its identity in thermodynamic processes
  - Does not disturb or interact with environment
  - Has uniform properties
  - Its pressure is always equal to that of ambient air



# Adiabatic parcel model

$$\gg \frac{d^2 z}{dt^2} = F_B = \frac{gT'}{T_0}$$

$$\gg \frac{d\theta_e}{dt} = 0$$

» Optionally, moisture too:

$$\gg \frac{dQ_v}{dt} = S_v$$

$$\gg \frac{dQ_w}{dt} = S_w$$

$$\gg \frac{dQ_r}{dt} = S_r - Q_r/\tau_{fall}$$

Example:

$$w dw = F_B dz \Rightarrow w^2 = w_{cb}^2 + 2 \int_{z_0}^z F_B dz$$

$$w_{max} = \sqrt{2 CAPE}$$

$$CAPE = \int_{LFC}^{ct} F_B dz$$



# Adiabatic parcel model

$$\gg \frac{d^2z}{dt^2} = F_B = \frac{gT'}{T_0}$$

$$\gg \frac{d\theta_e}{dt} = 0$$

$$\gg \theta_e = \theta_e(T, p) \Rightarrow T = \dots$$

Example:

$$wdw = F_B dz \Rightarrow w^2 = w_{cb}^2 + 2 \int_{z_0}^z F_B dz$$

$$w_{max} = \sqrt{2 CAPE}$$

$$CAPE = \int_{LFC}^{ct} F_B dz$$

» Assuming water saturation (conserve  $Q_T = Q_v + Q_w$ ):

$$\gg \frac{dQ_T}{dt} = -S_r$$

$$\gg Q_w = Q_T - Q_{v,s}$$

$$\gg \frac{dQ_r}{dt} = S_r - Q_r/\tau_{fall}$$



# Entraining parcel model (e.g. Donner 1993)

» Entrainment rate  $= E = \frac{1}{m} \frac{dm}{dt} \sim \text{constant}$

»  $\frac{d^2 z}{dt^2} = g \left( \frac{T_v'}{T_0} - Q_w - Q_r \right) - E w$

»  $\frac{dQ_T}{dt} = -S_r - E Q_T'$

»  $Q_w = Q_T - Q_{v,s}$

»  $\frac{dQ_r}{dt} = S_r - E Q_r - \frac{Q_r}{\tau_{fall}}$

»  $\frac{d\theta_e}{dt} = -E \theta_e'$



# 1-D CLOUD MODELS



# Vertical 1-D draft

- » Include interaction between dynamics and microphysics (e.g. Srivastava 1967)
- » Approach: solve Boussinesq eqns for conservation of momentum, heat, and mass of moisture for vertical motion

$$\frac{DU}{Dt} = g \left( \frac{T_v'}{T_0} - Q_w - Q_r \right)$$

$$\frac{DQ_v}{Dt} = S_v = E_v$$

$$\frac{DQ_w}{Dt} = S_w = -E_{v,1} - P$$

$$\frac{DQ_r}{Dt} + \frac{1}{\rho_0} \frac{\partial}{\partial z} (\rho_0 Q_r V) = S_r = -E_{v,2} + P$$

$$\frac{DT}{Dt} = -U \Gamma_s - LE_v/c_p$$

$$\frac{D}{DT} \equiv \frac{\partial}{\partial t} + U \frac{\partial}{\partial z}$$

Evaporation  
(or condensation)

$$E_v = E_{v,1} + E_{v,2}$$

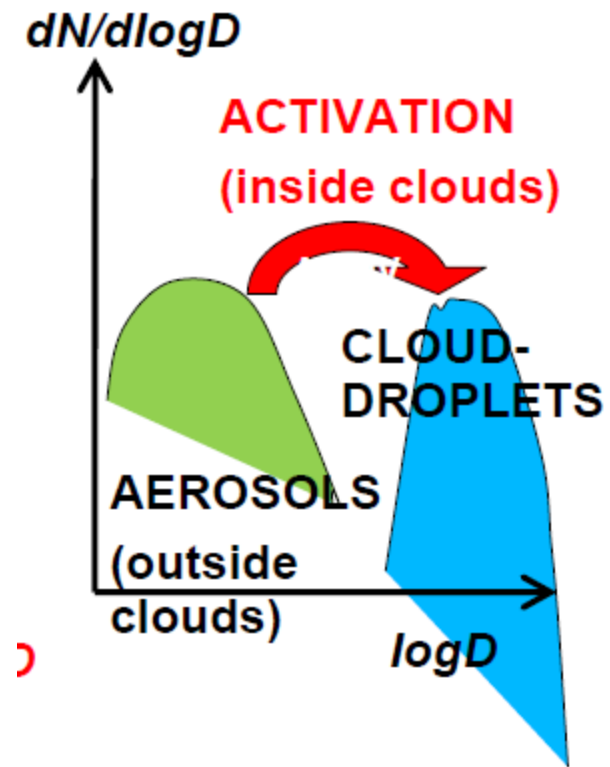


# Bulk microphysics

- » Kessler (1969) analysed drop size distributions (DSDs)
- » By approximating a mathematical form for DSDs (e.g. exponential), he derived:

- » Evaporation (or condensation)
- » Average fall-speed,  $V$
- » Precipitation production,  $P$ ,

- Some cloud-water converts spontaneously to rain when a threshold on  $Q_w$  is exceeded



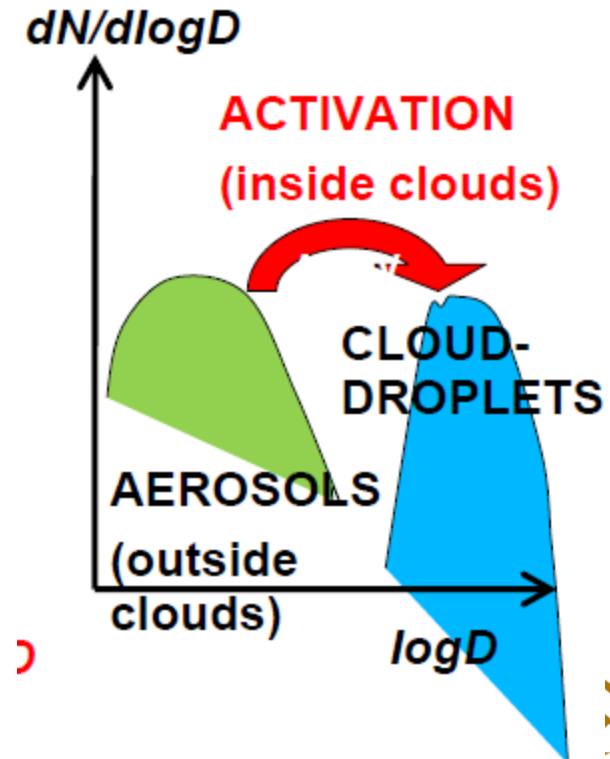
$$E_v = E_{v,1} + E_{v,2}$$





# Bin microphysics: more accuracy in treatment of coagulation and sedimentation

- » Danielson et al. (1972) explicitly accounts for DSDs and for ice size distributions
  - Stochastic coalescence predicted bin by bin
  - Concentration is explicitly predicted in each of many categories arranged logarithmically over size
    - » water drops: from 2 microns to 2.5 mm
    - » Ice: up to 20 mm



# Results: Case Study

- » Example: shower, a convective cell, warm climate (Srivastava 1967)
- » In first 10 mins, rain develops at expense of cloud-liquid, forming first near cloud-top
  - Updraft starts weakening, due to burden of rain
- » After about 20 mins, rain has descended, forming downdraft at low levels
  - updraft strengthens again



# Overview of 1D models

## » Advantages:

- Interaction of dynamics and microphysics treated
- Computationally cheap
- Good for analysis of microphysical processes

## » Disadvantages

- Crude treatment of dynamics (no shear)
- In reality, vertical shear controls storm structure, and there are downdrafts flanking updraft



# 2D CLOUD MODELS



- » Approach: solve Boussinesq equations for conservation of momentum, heat, and mass of air and moisture on a vertical grid ( $x, z$ )
  - Density constant,  $\rho_0(z)$ , except for  $F_B$  (Boussinesq)
  - Include convergence of turbulent fluxes,  $F$
  - Treat pressure and temperature as sum of basic state ( $p_0(z), T_0(z)$ ) and a perturbation ( $p'(x, z, t), T'(x, z, t)$ )
  - Convection started by warm bubble initially

$$\frac{D}{DT} \equiv \frac{\partial}{\partial t} + u \frac{\partial}{\partial x} + w \frac{\partial}{\partial z}$$



$$\frac{Du}{Dt} = F_u - \frac{1}{\rho_0} \frac{\partial p'}{\partial x}$$

$$\frac{Dw}{Dt} = g \left( \frac{T_v'}{T_0} - Q_w - Q_r \right) + F_w - \frac{1}{\rho_0} \frac{\partial p'}{\partial z}$$

$$0 = \frac{\partial(\rho_0 u)}{\partial x} + \frac{\partial(\rho_0 w)}{\partial z}$$

$$\frac{DT}{Dt} = -\Gamma_s w + F_T + S_T$$

$$\frac{DQ_v}{Dt} = S_v + F_v$$

$$\frac{DQ_w}{Dt} = S_w + F_w$$

$$\frac{DQ_r}{Dt} + \frac{1}{\rho_0} \frac{\partial}{\partial z} (\rho_0 Q_r V) = S_r + F_r$$



# Results: Case Study

- » Takeda (1971) used above 2D model but with bin microphysics, treating stochastic coalescence and breakup
- » Type 1: weak vertical shear, moderate instability
  - Clouds develop in-cloud downdraft due to precipitation burden and evaporative cooling
  - Cold pool near surface spreads and triggers new cell
  - New clouds develop around dissipating cloud
- » Type 2: strong shear, moderate instability
  - Downdraft forms on downshear side
  - No new cells triggered, cloud is short-lived



# Overview of 2D model

## » Advantages:

- Effects from vertical shear on longevity and intensity of storm simulated
- Cheaper than 3D

## » Disadvantages:

- Vertical motions grossly distorted
- Vertical pressure perturbation forces grossly overestimated
- Turbulence ?
- Forecasting ?





# 3D CLOUD MODELS



# Need for 3D model for realism

» In reality,

- wind speed and direction change with height:
- Vortices are advected, tilted and stretched in 3D (e.g. tornadoes), updrafts rotate
- Outflow in downdrafts can interact with ambient flow, forming multicell storms
- PPGF and updraft speeds differ between 2D and 3D
- Clouds act as barriers to ambient flow at some (near steering) levels, move with the wind at other levels



- » Approach: solve numerically 3D version of Boussinesq equations for 2D models

$$\frac{D}{DT} \equiv \frac{\partial}{\partial t} + u \frac{\partial}{\partial x} + v \frac{\partial}{\partial y} + w \frac{\partial}{\partial z}$$



# Results:

- » Splitting of supercells simulated by Wilhelmson and Klemp (1978)
  - Sensitivity test shows splitting is due to rain
  - Right-moving storms are more common after splitting (than left-moving ones) because ambient flow turns clockwise with height usually
    - » Low-level convergence due to downdrafts sustains the storm and the downdrafts are promoted by mid-level inflow from south, which is linked to such a sounding
- » Tornadoes simulated and explained in terms of intensification of mesovortex (Klemp *et al.* 1981)



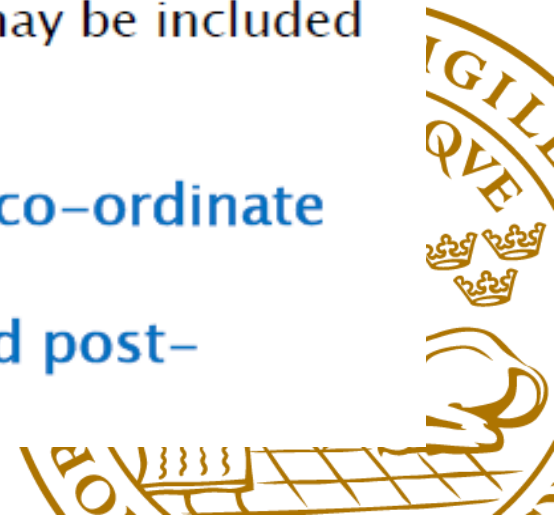
**EXAMPLE OF MODELING  
SYSTEM FOR RESEARCH AND  
FORECASTING**



# Example of 3D model: Weather, Research and Forecasting (WRF)

## Outline of WRF

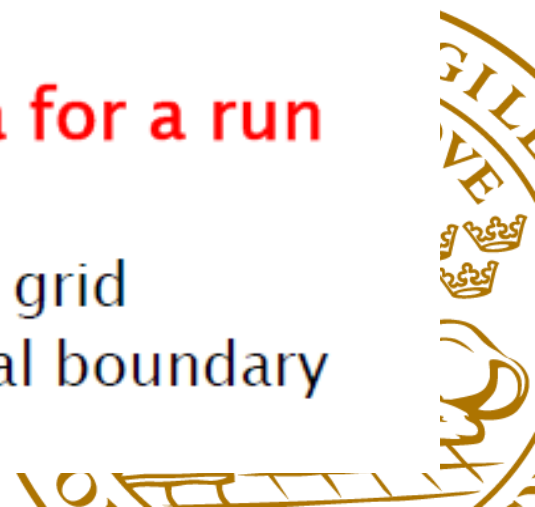
- ▶ **Two forms of WRF:**
  - Advanced Research WRF (ARW)
  - Non-hydrostatic Mesoscale Model (NMM)
- ▶ **Both are Eulerian mass dynamical cores**
  - terrain-following vertical co-ordinates
  - non-hydrostatic (sound and gravity waves may be included by high-resolution solution of ODEs)
- ▶ **Pressure closely related to their vertical co-ordinate**
- ▶ **Pre-processing, main model running and post-processing elements in both**



# Components of WRF modeling system

## Initialisation of WRF simulation

- ▶ **WRF Pre-processing System (WPS) prepares data for a run**
  - Real observational data interpolated by WPS onto model grid, if numerical weather prediction (NWP) runs are to be done
- ▶ **WRF Model also prepares the data for a run (“real.exe” and “ideal.exe”) :**
  - Hydrostatic balance of data on model grid
  - Creates data-files for lateral and initial boundary conditions



# Components of WRF modeling system

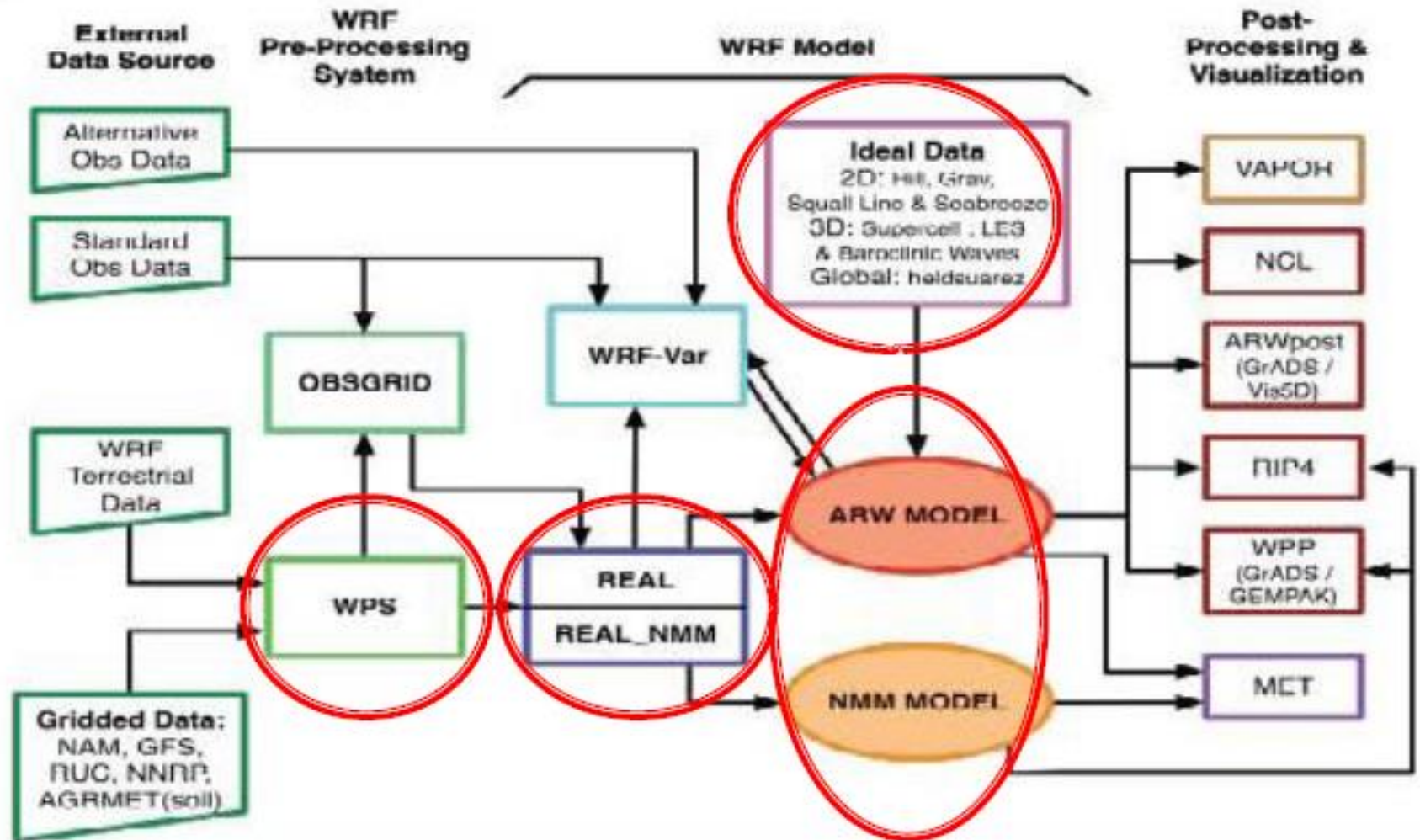
## WRF Model run and post-processing:

- ▶ **WRF Model (ARW or NMM) solves ODEs of physical and dynamical laws so as to simulate the atmosphere (“wrf.exe”)**
  - reads in input data (processed previously), and initialises variables/arrays
  - Integrates ODES, creating output
- ▶ **Graphics and Verification tools**
  - (e.g. RIP4, WPP, NCL)





# Map of WRF modeling system



# Dynamics of ARW WRF Model

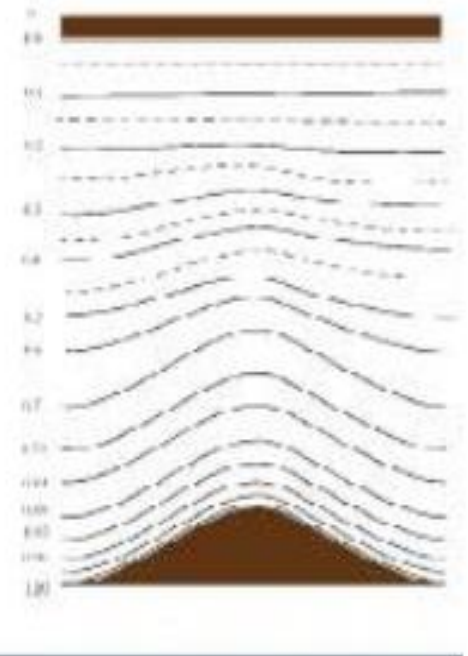
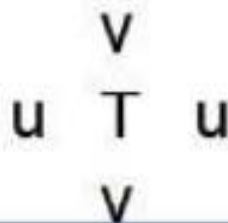
Key features:

- Fully compressible, non-hydrostatic (with hydrostatic option)
- Mass-based terrain following coordinate,  $\eta$

$$\eta = \frac{(\pi - \pi_t)}{\mu}, \quad \mu = \pi_s - \pi_t$$

where  $\pi$  is hydrostatic pressure,  
 $\mu$  is column mass

- Arakawa C-grid staggering



# WRF as cloud model

Phenomena occur on many scales, some too small to resolve on model grid

*WRF AS CLOUD-SYSTEM RESOLVING MODEL (CSR)*

*NOT RESOLVED BY WRF'S RESOLUTION OF  $\Delta X = 2 \text{ km}$*

$L_s \backslash T_s$	1 month	1 day	1 hour	1 minute	1 second	
10,000 km	Equatorial waves in the tropics					Planetary Scale
2,000 km		Baroclinic waves				Synoptic scale
200 km		Fronts, Tropical cyclones				Meso Scale $\alpha$
20 km			Orographic effects, land-sea winds			Meso Scale $\beta$
2 km			Thunderstorms, gravity waves, urban heat islands			Meso Scale $\gamma$
200 m			Tornadoes, convection			Micro Scale $\alpha$
20 m				Dust devils, thermals		Micro Scale $\beta$
					Small scale turbulence	Micro Scale $\gamma$
	Macroscale		Mesoscale		Microscale	

**PARAMETRIZED PROCESSES**



# WRF as regional model

Phenomena occur on many scales, some too small to resolve on model grid

*WRF AS REGIONAL (e.g. HURRICANE) MODEL*

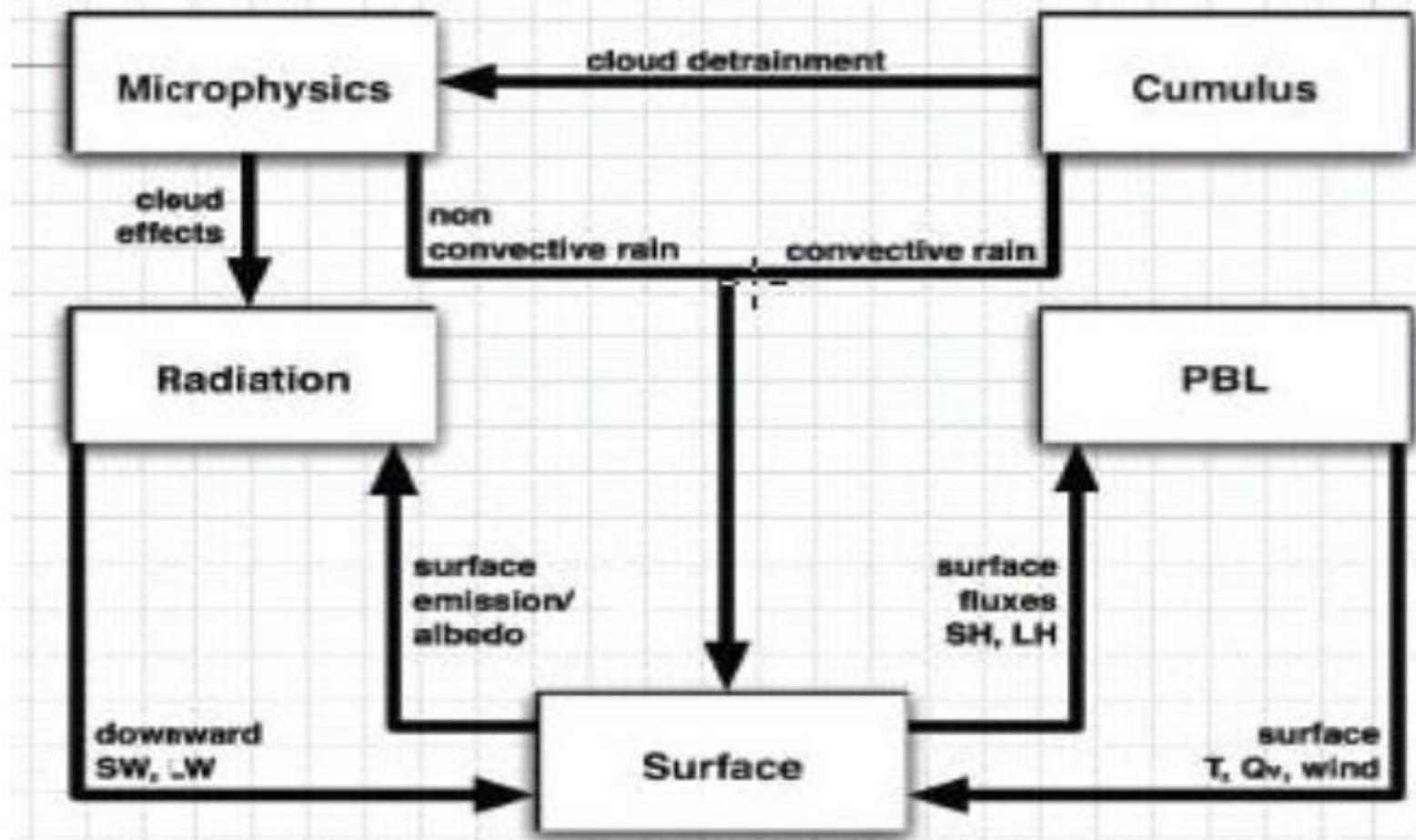
*NOT RESOLVED BY WRF'S RESOLUTION OF  $\Delta X = 50 \text{ km}$*

$L_x \backslash T_s$	1 month	1 day	1 hour	1 minute	1 second	
10,000 km	Equatorial waves in the tropics					Planetary Scale
2,000 km		Baroclinic waves				Synoptic scale
200 km		Fronts, Tropical cyclones				Meso Scale $\alpha$
20 km			Orographic effects, land-sea winds			Meso Scale $\beta$
2 km			Thunderstorms, gravity waves, urban heat islands			Meso Scale $\gamma$
200 m			Tornadoes, convection			Micro Scale $\alpha$
20 m				Dust devils, thermals		Micro Scale $\beta$
					Small scale turbulence	Micro Scale $\gamma$
	<b>Macroscale</b>		<b>Mesoscale</b>		<b>Microscale</b>	

*PARAMETRIZED PROCESSES*



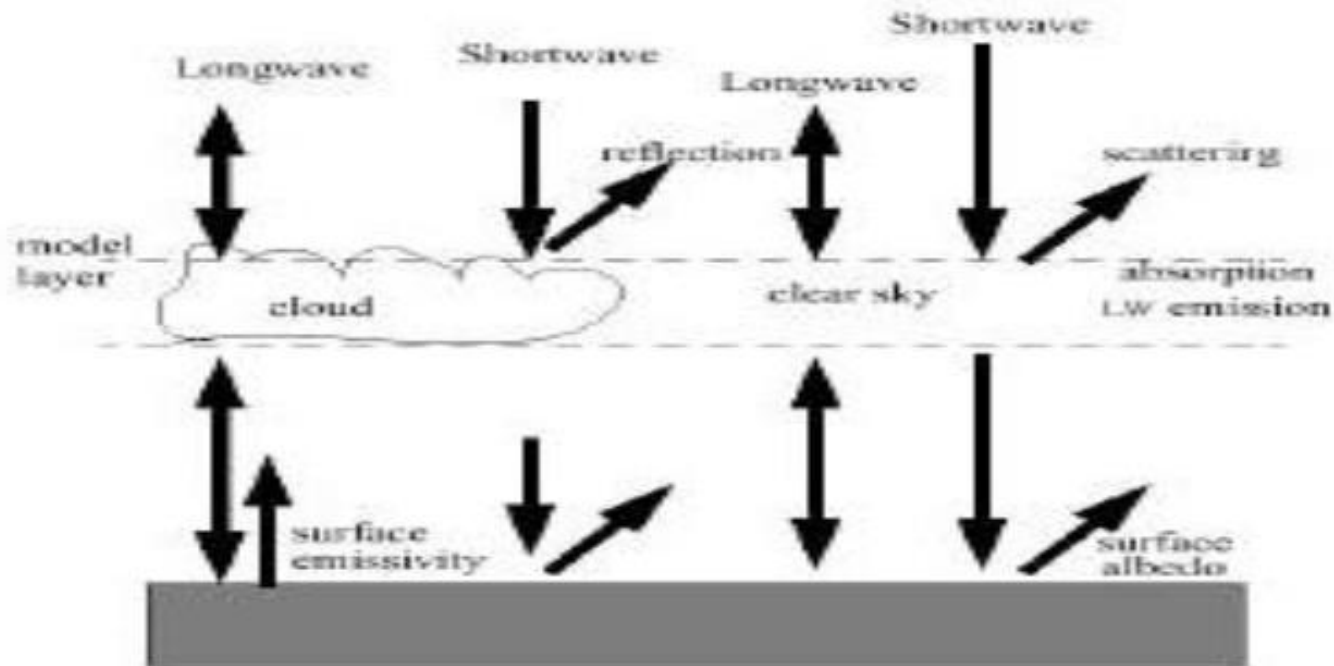
# Map of parameterizations when all are used (e.g. WRF as regional model)



# WRF Parametrisations: Radiation

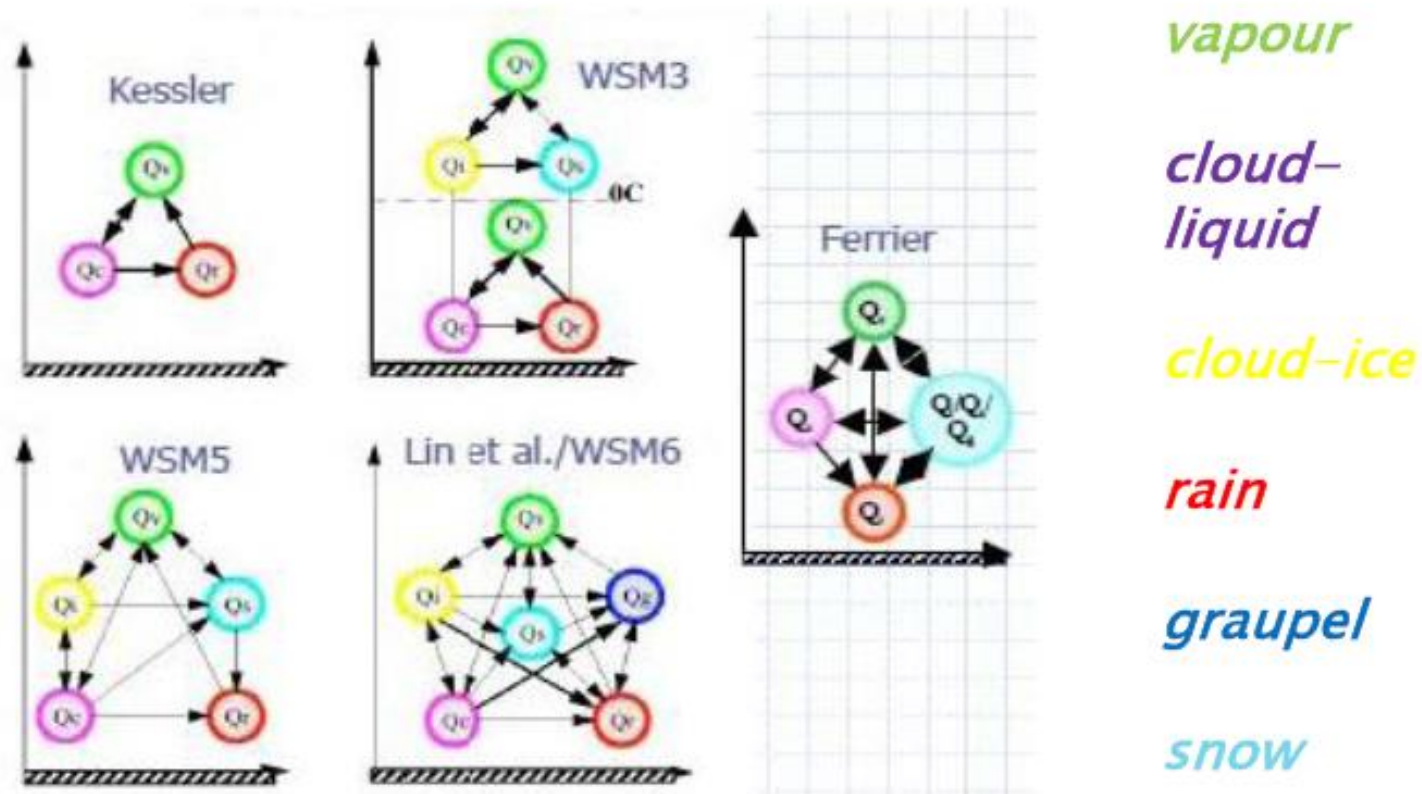
## Radiative Transfer in Atmosphere:

- ▶ Models always treat solar (shortwave [SW]) and terrestrial (longwave [LW]) radiation from Sun and Earth separately, since there is no overlap



# Options: microphysics schemes

## Multiple species of hydrometeor




# Example: Morrison scheme

## ▶ Usual 5 species of hydrometeor:

- Cloud-ice, snow, graupel, cloud-liquid, rain

## ▶ 2-moment treatment of some species

- $x$ -th species has a size distribution,  $dN_x (\#/m^3) = n_x(D) dD$
- both total mass and number of particles, per  $m^3$ , are predicted
  - $N_x = \int n_x dD$  (0-th moment)
  - $Q_x \propto \int D^3 n_x dD$  (3<sup>rd</sup> moment)
  - Prediction of  $N_x$  and  $Q_x$   mean size of particles and  $n_x$  predicted

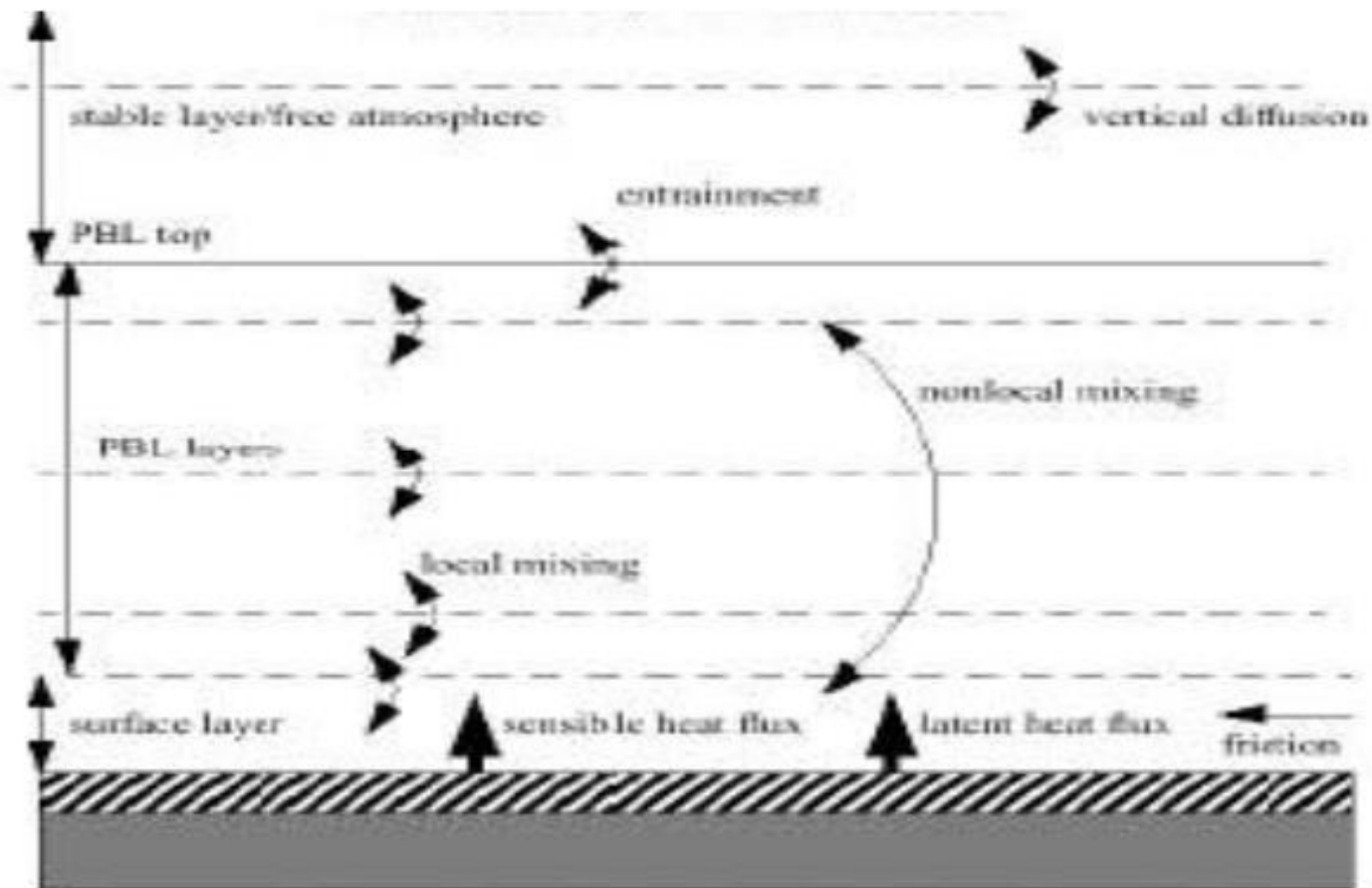
## ▶ Advantage of 2-moment approach: in nature, cloud properties determined by mean size of cloud-particles

- Cloud properties are predicted





# PBL scheme (e.g. $bl\_pbl\_physics = 1$ ): vertical turbulent fluxes of heat and moisture



# SUMMARY



- » Complex mechanisms elucidated by models
- » Parcel models can elucidate microphysical processes
- » 1D, 2D and 3D models include an increasing range of mechanisms
- » Modeling systems (e.g. WRF) have flexibility for choice of any resolution and of corresponding parameterizations



Obrigado

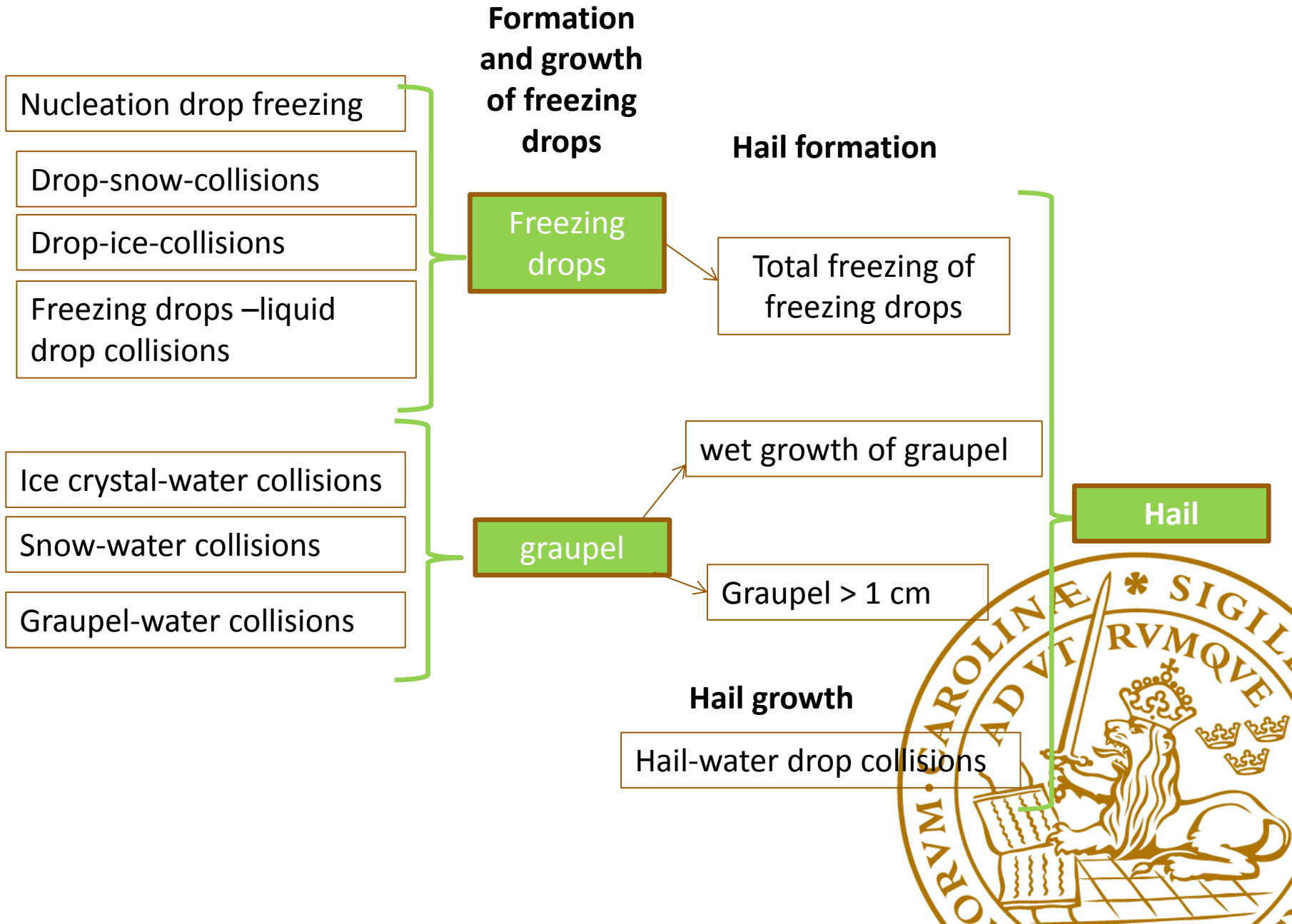


Example: Very high resolution (about 0.5 km) 2D model with bin microphysics

- explicit prediction of size distributions and cloud-processes



# New transformation of hydrometeors during hail formation in HUCM:



# Dynamics of ARW WRF Model

## Key features:

- 3rd-order Runge-Kutta time integration scheme
- High-order advection scheme
- Scalar-conserving (positive definite option)
- Complete Coriolis, curvature and mapping terms
- Two-way and one-way nesting



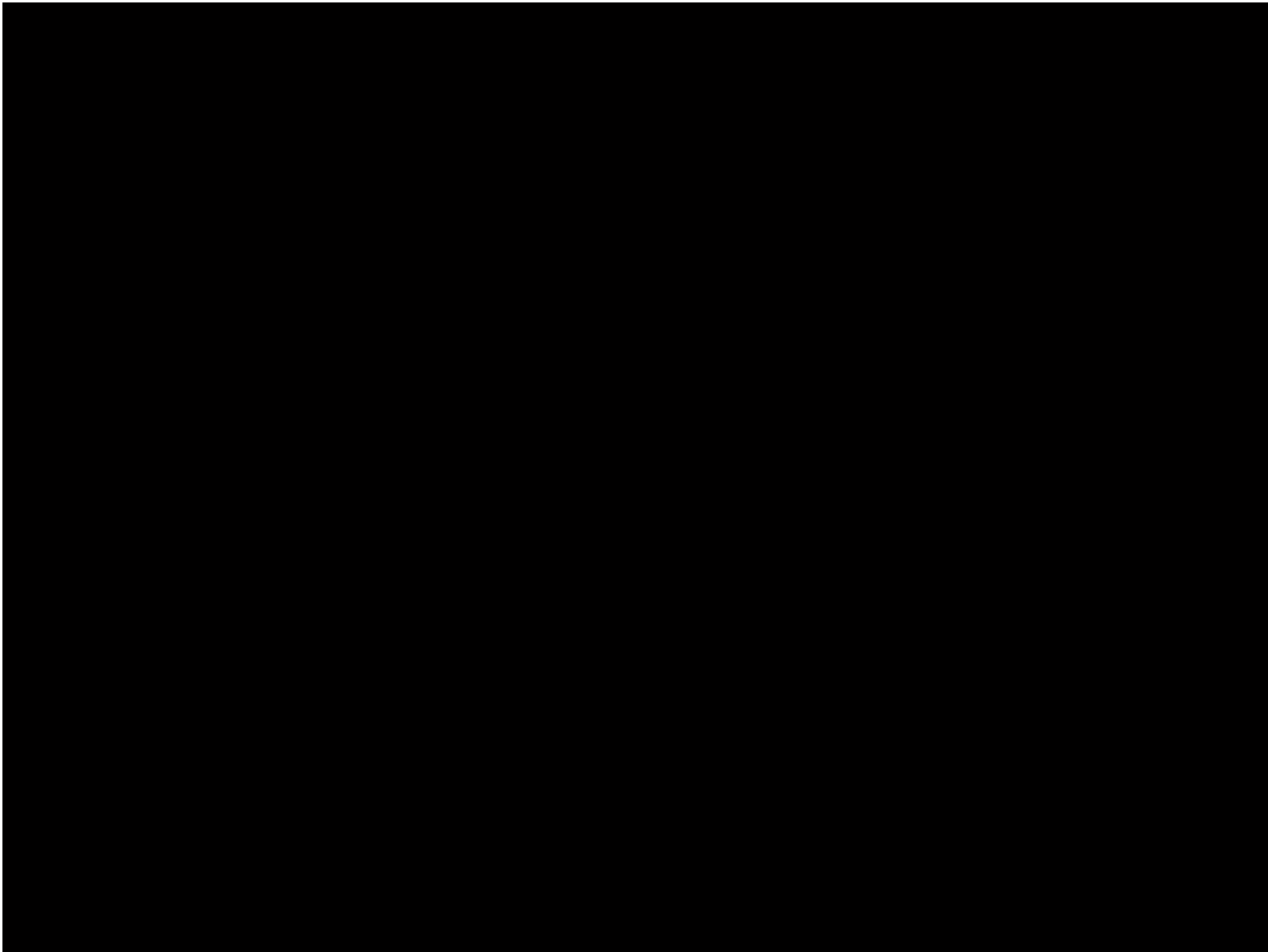
# Dynamics of ARW WRF Model

## Key features:

- Choices of lateral boundary conditions suitable for real-data and idealized simulations
  - Specified, Periodic, Open, Symmetric, Nested
- Full physics options to represent atmospheric radiation, surface and boundary layer, and cloud and precipitation processes
- Grid-nudging and obs-nudging (FDDA)
- New Digital Filter Initialization option







- » Type 3: low-level jet, with strong opposite shears above and below it
  - Precipitation and updraft are both inclined in direction of low-level shear at low levels,
  - Updraft has opposite tilt aloft
  - Cold pool from downdraft spreads out, triggering ascent near base of original updraft
  - Long-lived cloud

» Other 2D models: Farley and Orville (1986), Khain et al. (2004)



# Turbulence

- ▶ When fluid flow is turbulent, its elements move irregularly and do not follow the direction of the mean flow
- ▶ Turbulent eddies cause random fluctuations of advected quantities around their mean ( $\langle \rangle$ ) values

$$X = \langle X \rangle + X'$$

*MEAN (e.g. RESOLVED ON GRID)*      *EDDY (e.g. SUB-GRIDSACLE)*

- ▶ Turbulence involves interactions and exchange of energy between motions of different scales
- ▶ Momentum equation,  $D\mathbf{v}_H/Dt = \Sigma_i \mathbf{F}_i$ , can be modified for grid-box average quantities, with an **extra eddy stress term**:

$$\circ \quad D\langle \mathbf{v}_H \rangle / Dt = \Sigma_i \langle \mathbf{F}_i \rangle + (1/\rho) \partial [\rho \langle w' \mathbf{v}_H' \rangle] / \partial z$$

*RESOLVED ON GRID*      *EFFECT FROM SUB-GRIDSACLE TURBULENCE (PARAMETERIZATION)*

▶ Similarly, the (1<sup>st</sup> Law) energy eqn,  $D\theta/Dt = \Sigma_i S_i$ , becomes

$$\circ D\langle\theta\rangle/Dt = \Sigma_i \langle S_i \rangle + (1/\rho) \partial [\rho \langle w' \theta' \rangle] / \partial z$$

*RESOLVED ON GRID*

*EFFECT FROM SUB-GRIDSCALE TURBULENCE  
(PARAMETERIZATION)*

▶ Vertical turbulent fluxes of heat and momentum are  $\rho \langle w' v_H' \rangle$  and  $\rho \langle w' \theta' \rangle$

▶ *Turbulent mixing transports heat and momentum down the gradient of mean temperature and mean momentum*

$$\bullet \rho \langle w' v_H' \rangle \sim -\rho K_m \partial \langle v_H \rangle / \partial z$$

$$\bullet \rho \langle w' \theta' \rangle \sim -\rho K_h \partial \langle \theta \rangle / \partial z$$

▶ PBL/turbulent mixing parameterizations predict  $K_{m/h}(z)$  and the turbulent fluxes of heat, moisture and momentum

◦  $K$  varies strongly with  $z$  in surface layer (lowest 10% of PBL)

◦ In surface layer:  $K_m \propto \partial \langle v_H \rangle / \partial z$  and  $K_h \propto \partial \langle \theta \rangle / \partial z$

