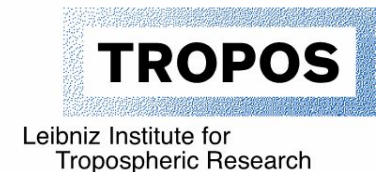


Atmospheric Aerosol Physics, Physical Measurements, and Sampling

Definitions & Mechanical Properties

São Paulo School of Advanced Science on Atmospheric Aerosols:
properties, measurements, modeling, and effects on climate and health



Definitions

General Definitions

Definition of an aerosol

Solid and /or liquid particles suspended in a gas

Coarse Particles

Particles >1 μm in diameter

Fine Particles

Particles <1 μm in diameter

Accumulation mode range 100-1000 nm

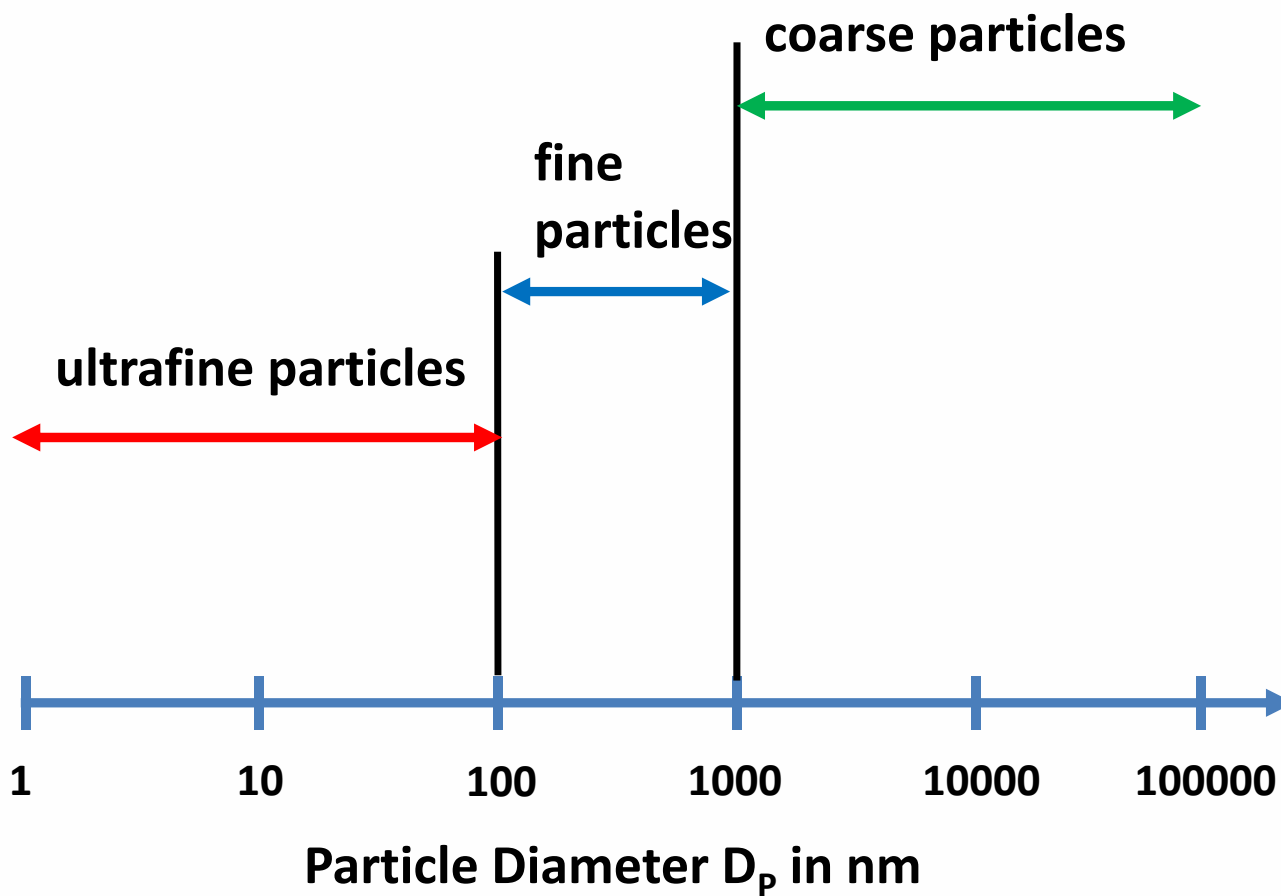
Ultrafine Particles

Particles < 100 nm in diameter

Aitken mode range 10-100 nm

Nucleation mode range 1-10 nm

Particle Size Ranges



Particle Size

Definition

$$1 \text{ nm} < D_p < 100 \text{ }\mu\text{m}$$

$$10^{-9} \text{ m} < D_p < 10^{-4} \text{ m}$$

Micro-Range

1 nm particle

350 nm particle

2.5 μm particle

100 μm particle

Macro-Range

0.1 mm tip of a needle

3.5 cm ping-pong ball

25 cm soccer ball

10 m balloon

Shape & Concentrations

Particle Shape

Aerosol particles are normally non-spherical.

However, particles are often assumed to be spheres for a simpler description and use (equivalent diameter).

Aerosol particles with extreme shapes should not be described as spherical particles.

Examples for non-spherical particles

- Asbestos fibers
- Chain agglomerates

Examples for “spherical particles”

- Droplets
- Fly ash particles
- Inorganic salt particles (crystals)
- Compact particles

Particle Concentrations

- The **particle number concentration** is described by the parameter N .
- It is defined by the number of particles per volume unit, and given in $\#/cm^3$.

Other concentrations:

- | | |
|---------------------------------------|------------------------|
| - Particle surface area concentration | S [$\mu m^2/cm^3$] |
| - Particle volume concentration | V [$\mu m^3/cm^3$] |
| - Particle mass concentration | M [$\mu g/m^3$] |

- The mass concentration can be calculated from the volume concentration and the particle density ρ_p .
- The particle density is given in $[g/cm^3]$.

Reynolds Numbers

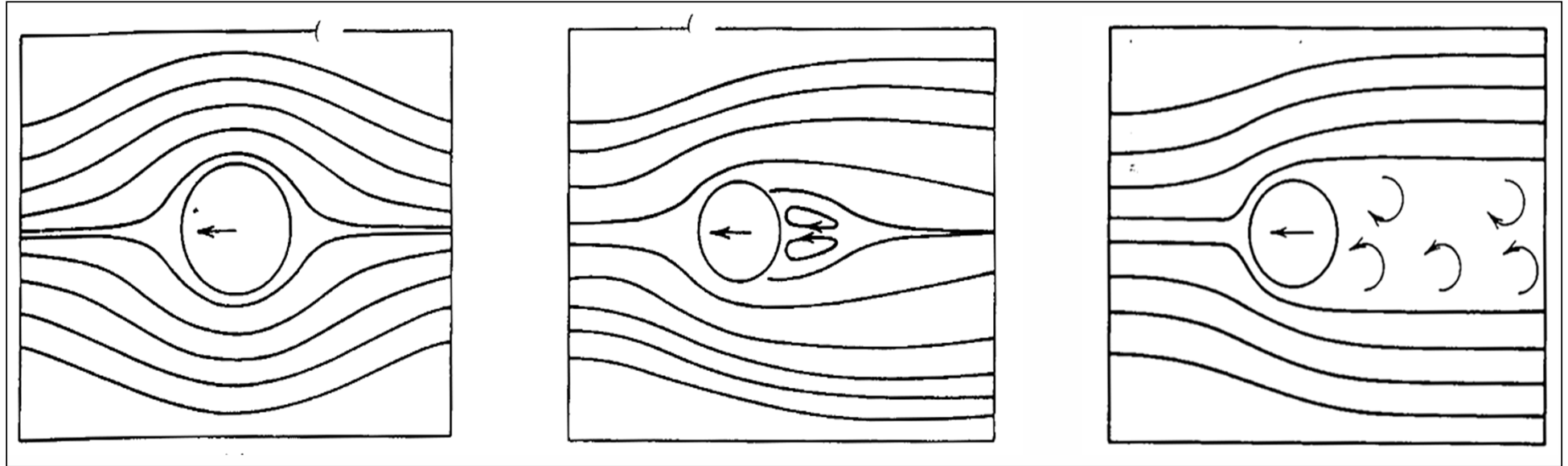
Particle Reynolds Number

The **Particle-Reynolds-Number** is an important quantity for the characterization of the mechanical properties of aerosol particles.

$$\text{Re}_p = \frac{\rho_G u_p D_p}{\eta}$$

- It characterizes the flow around an aerosol particle.
- Equal Particle-Reynolds-Numbers imply the same pattern of stream lines in the vicinity of particles with different size and in different gases.
- It is the most important property for the determination of the drag force a gas exerts on a suspended particle.

Flow around a sphere



Laminar flow, $Re = 0.1$

Turbulent flow, $Re \approx 2$

Turbulent flow, $Re \approx 250$

Flow-Reynolds-Number

The **Flow-Reynolds-Number** depends mainly on the flow rate and the tube diameter

$$\text{Re}_{\text{flow}} = \frac{\rho_{\text{gas}} \cdot \bar{u}_{\text{flow}} \cdot D_{\text{pipe}}}{\eta}$$

- ρ_{gas} ... gas density
- u_{flow} ... flow velocity
- D_{pipe} ... tube diameter
- η ... dynamic viscosity

Forces & Stokes Law

External Forces

External forces on a particles will result in a macroscopically directed particle motion.

Examples for external forces:

- Gravitational force

$$\vec{F}_g = \frac{\pi}{6} D_p^3 \cdot \rho_p \cdot \vec{g} \cdot \left(1 - \frac{\rho_G}{\rho_p}\right)$$

- Electrical force

$$\vec{F}_e = n_e \cdot e \cdot \vec{E}$$

- Thermophoresis

$$\vec{F}_{th} = -\frac{3 \cdot \pi \cdot \eta^2 \cdot D_p \cdot K_{th} \cdot \nabla T}{\rho_G T}$$

Newton's Law

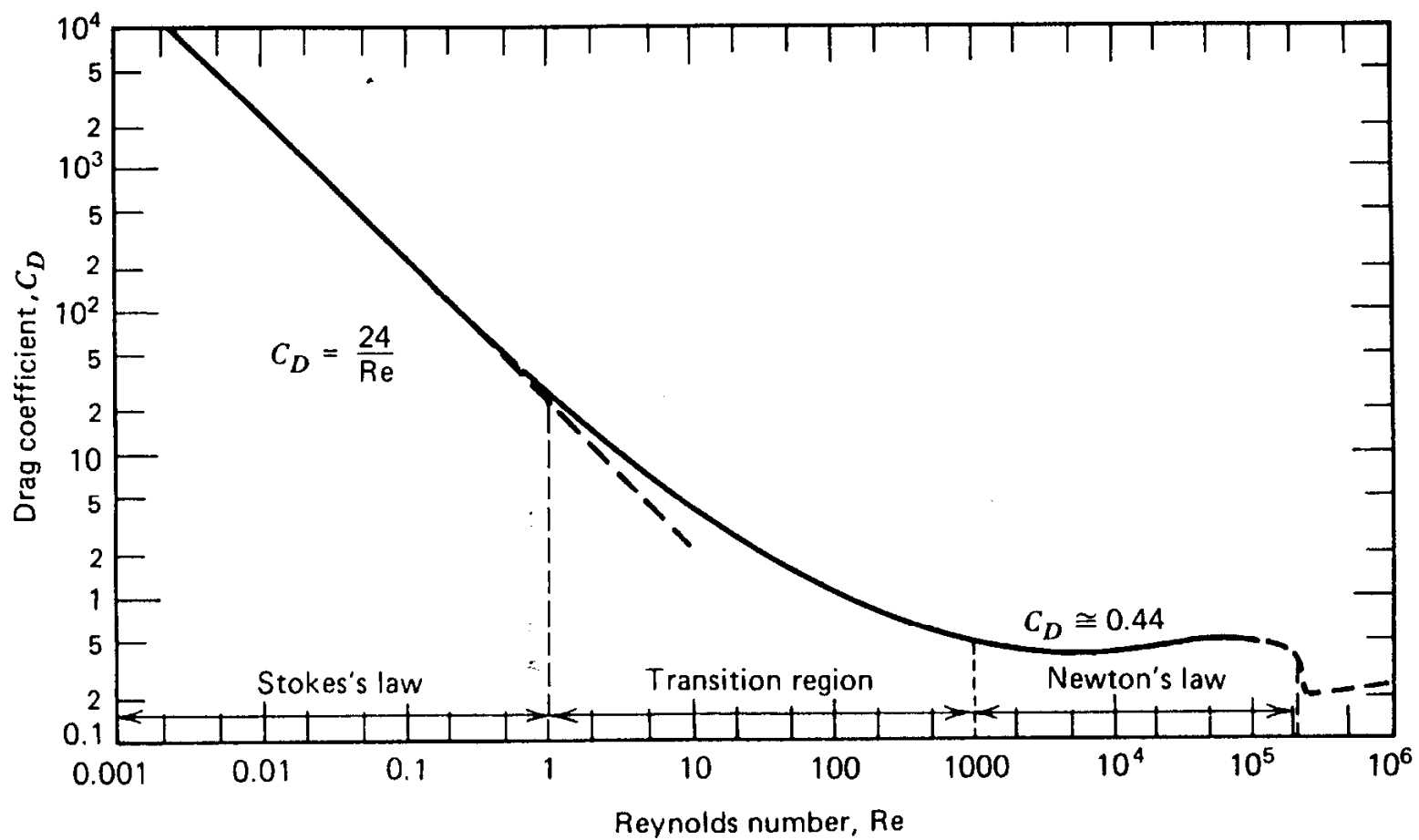
Newton's Law describes the drag force as stagnant gas exerts on a moving body, e.g. a sphere.

$$F_D = \frac{\pi}{8} \cdot \rho_G \cdot u_P^2 \cdot C_D \cdot D_P^2$$

- This general equation is applicable over a wide range of Reynolds-Numbers ($Re = 10^3 - 10^5$).
- In this regime, the drag coefficient C_D is nearly constant.
- For Reynolds-Numbers $Re < 1000$, the drag coefficient is a function of Reynolds-Number.

$$C_D = \frac{24}{Re} \left(1 + \frac{Re^{2/3}}{6} \right)$$

- In the regime $3 < Re < 400$, the introduced error is less than 2 % and up to $Re = 1000$ less than 10 %.



Drag coefficient versus Reynolds number for spheres

Figure: Hinds: Aerosol Technology: Properties, Behavior, and Measurement of Airborne Particles

Stokes' Law

Most particle movement takes place at low Particle-Reynolds-Numbers, as both, the flow velocity and the particle diameter are usually small.

Stokes' Law is a special solution of the momentum, i.e. the Navier-Stokes-equation.

Therefore, the following assumptions are made:

- incompressible flow
- steady state
- gas velocity equal to zero at the particle surface (no slip boundary)

The drag coefficient can be determined applying Newton's Law:

$$C_D = \frac{24}{\text{Re}}$$

The drag force results in:

$$\vec{F}_D = 3\pi \cdot \eta \cdot \vec{u}_p \cdot D_p$$

The temperature dependency of the viscosity can be described as follows:

$$\eta = \eta_0 \left(\frac{T}{T_0} \right)^{3/2} \left(\frac{T_0 + 110.4\text{K}}{T + 110.4\text{K}} \right)$$

Cunningham Correction Factor

For particle diameters $D_p < 10000$ nm, the gas velocity at the particle surface is not equal to zero, which results in a reduced drag force.

This effect is accounted for by the **Cunningham correction factor**

$$C_C = 1 + \frac{\lambda}{D_p} \left(2.514 + 0.8 \cdot \exp\left(-0.55 \frac{D_p}{\lambda}\right) \right)$$

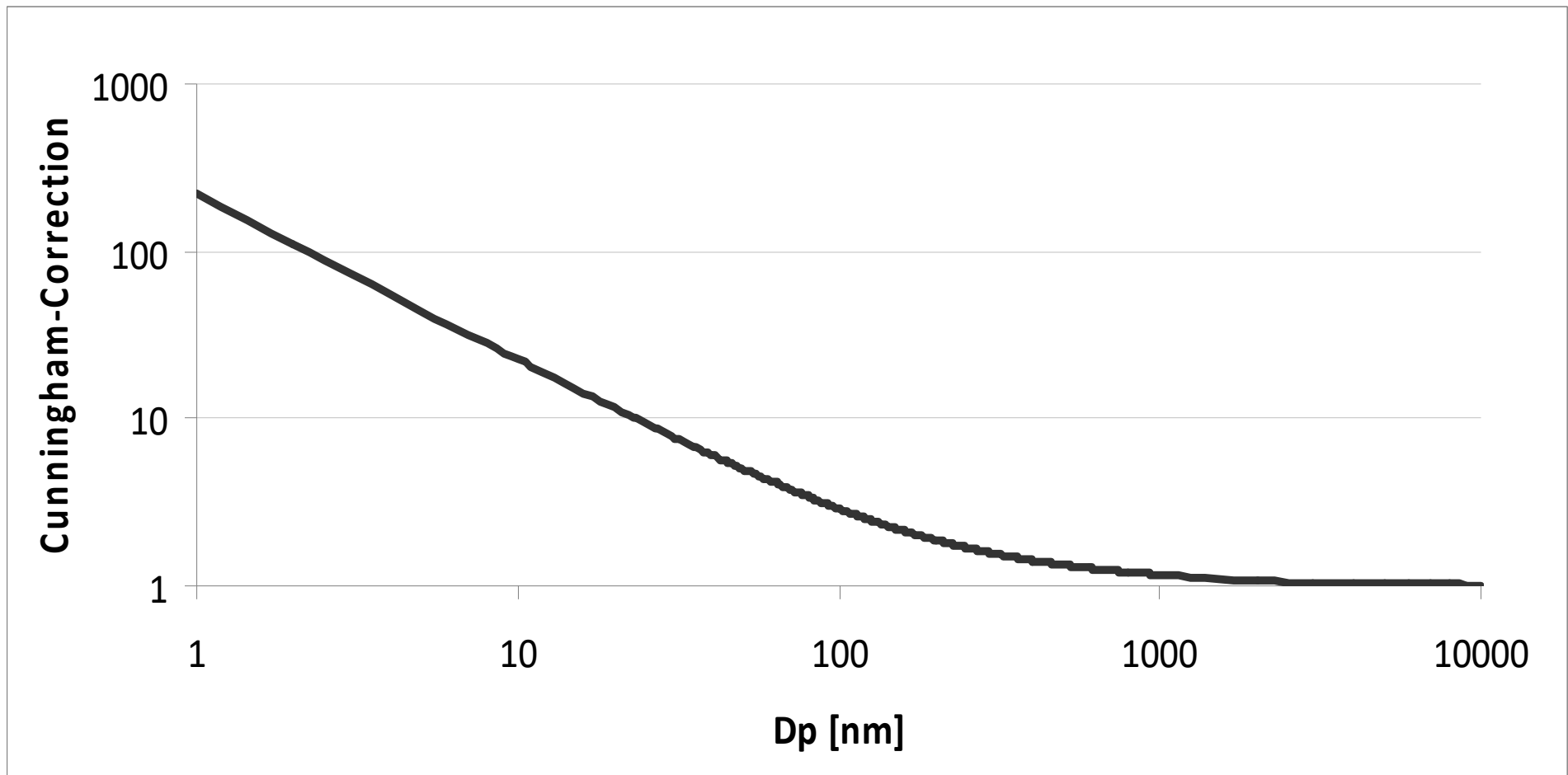
The **drag force** then becomes:

$$\vec{F}_D = \frac{3\pi \cdot \eta \cdot \vec{u}_p \cdot D_p}{C_C}$$

The Cunningham correction factor was determined empirically via the determination of the settling velocity of particles with known size and density.

For the pressure & temperature dependency of the Cunningham correction factor, the mean free path has to be corrected according to:

$$\lambda = \lambda_0 \left(\frac{T}{T_0} \right)^2 \left(\frac{p_0}{p} \right) \left(\frac{T_0 + 110.4\text{K}}{T + 110.4\text{K}} \right)$$



Cunningham correction factor as function of particle size

Mobility & Settling

Mechanical Mobility

The **drag force** on a particle in an uniform motion results in:

$$\vec{F}_D = \frac{3\pi \cdot \eta \cdot \vec{u}_p \cdot D_p}{C_C}$$

In Stokes' Law the drag force is directly proportional to the relative velocity between the particle and the gas. This fact can be used to introduce the **mechanical mobility** B :

$$B = \frac{\vec{u}_p}{\vec{F}_D} = \frac{C_C}{3\pi \cdot \eta \cdot D_p}$$

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Sedimentation Velocity

An important application of Stokes' law is the determination of the **sedimentation velocity** u_s of aerosol particles. In this case, the drag forces F_D is equal to the gravitational force F_G acting on the particle.

$$\vec{F}_D = \vec{F}_G$$
$$\frac{3\pi \cdot \eta \cdot \vec{u}_s \cdot D_P}{C_C} = \frac{\pi \cdot \rho_P \cdot D_P^3 \cdot \vec{g}}{6} \left(1 - \frac{\rho_G}{\rho_P}\right)$$

If the gas density is small compared to the particle density, the sedimentation velocity u_s can be calculated as follows:

$$\vec{u}_s = \frac{\rho_P D_P^2 C_C \vec{g}}{18\eta}$$

Settling velocity density = 1	
Dp (nm)	Us (m/s)
1	6,67E-09
10	6,82E-08
100	8,73E-07
1000	3,49E-05
10000	3,03E-03
100000	2,99E-01

Non-Spherical Particles

Non-Spherical Particles

The equations presented up to now are based on the assumption of a spherical particle shape.

Liquid droplets are spherical, but most of the aerosol particles are non-spherical.

The actual form (cubes, fibers, agglomerates) of a particle however affects the drag force and consequently e.g. the sedimentation velocity.

This is accounted for by introducing a **dynamic shape factor** into Stokes' Law:

$$\vec{F}_D = \frac{3\pi \cdot \eta \cdot \vec{u}_P \cdot D_{P,ve}}{C_C} \cdot \chi$$

The resulting mechanical mobility and sedimentation velocity are:

$$B = \frac{\vec{u}_P}{\vec{F}_D} = \frac{C_C}{3\pi \cdot \eta \cdot D_{P,ve} \cdot \chi}$$

$$\vec{u}_s = \frac{\rho_P \cdot D_{P,ve}^2 \cdot C_C \cdot \vec{g}}{18\eta \cdot \chi}$$

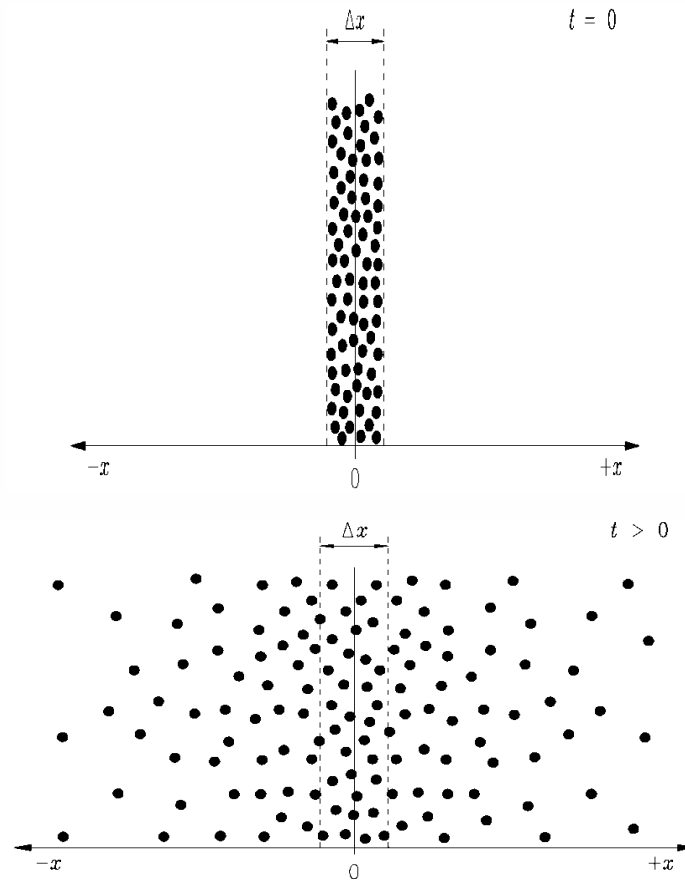
Shape factors

Shape	Dynamic Shape Factor
Sphere	1.00
Cube	1.08
Cluster chain of 4 spheres	1.32
Quartz	1.36
Sand	1.57

Table: Numbers taken from Hinds: Aerosol Technology: Properties, Behavior, and Measurement of Airborne Particles

Diffusion

Brownian Motion of Aerosol Particles



Hinds: Aerosol Technology: Properties, Behavior, and Measurement of Airborne Particles

Particle Diffusion

- The particle diffusion results from interactions between particles and gas molecules.
- Due to the impulse exchange molecules and particles, the Brownian motion of the molecules is transferred to the particles.
- The resulting particle motion is then called **Brownian particle motion**.
- A measure of the Brownian particle motion is the particle diffusion coefficient D .
- The Brownian particle motion is macroscopically non-directional.

$$D = k \cdot T \cdot B$$

Stokes Number & Relaxation Time

Stokes Number & Relaxation Time

The Stokes number characterizes the particle inertia in a flow

$$\text{Stk} = \frac{\tau \cdot u_0}{D_{\text{pipe}}}$$

with

$$\tau = \frac{\rho_P \cdot D_P^2 \cdot C_C}{18\eta}$$

τ ... relaxation time
 u_0 ... wind velocity
 D_{pipe} ... tube diameter

The Stokes Number is the ratio between the particle stopping distance to characteristic dimensions of the flow profile.

Example

Particle diameter nm	Relaxation time s	Stopping distance m	Stokes number
10	6,95E-09	9,23E-09	2,31E-06
100	8,90E-08	1,18E-07	2,95E-05
1000	3,56E-06	4,72E-06	1,18E-03
10000	3,09E-04	4,11E-04	1,03E-01
100000	3,05E-02	4,04E-02	1,01E+01
Density: ρ_p	2000 kg/m ³		
Tube diameter: D_t	0.004 m		
Tube velocity: u_t	1.33 m/s		
	(5 l/min in ¼" tube)		